

## Design of Concrete Structure-I

Plain cement concrete: plain cement concrete is a hardened mass obtained from a mixture of cement, sand, gravel and water in definite proportions. These ingredients are mixed together to form a plastic mass which is poured into desired shape moulds <sup>called</sup> as forms. This plastic mass hardens on setting and we get plain cement con.

The hardening of this mixture is caused by a chemical reaction between cement and water.

Reinforced cement concrete: - plain cement concrete has very low tensile strength. To improve tensile strength of concrete, some sort of reinforcement is needed which can take up the tensile stresses developed in the structure. The most common type of reinforcement is in the form of steel bars which are quite strong in tension.

The reinforcing steel is placed in the forms and fresh concrete is poured around it. This solidified composite mass is called a reinforced cement concrete and is abbreviated as R.C.C. Thus "Reinforced cement-concrete is a composite material which is made up of concrete and steel reinforcement.

The composite action of steel and concrete in a reinforced concrete section is dependent on the following imp. factor

- (i) The bond bet steel and concrete

- (ii) prevention of corrosion of steel bars embedded in the concrete.
- (iii) practically equal thermal expansion of both concrete and steel.

Advantages & disadvantages of R.C.C.: There are the following types of the advantages -

1. R.C.C has a very good strength in tension as well as compression

- ② Durability - R.C.C. structures are durable if designed and laid properly. Then they can last up to 100 years.
- ③ The steel reinforcement impart durability to the R.C.C. structure.
- ④ R.C.C. is cheaper as compared to steel and prestressed concrete.
- ⑤ R.C.C. is almost impermeable to moisture.
- ⑥ Properly designed R.C.C. structures are extremely resistant to earth quakes.

There are following disadvantages -

- ① R.C.C. structures are heavier than structures of other materials like steel, wood and glass etc.
- ② R.C.C. needs a lot of formwork, centering and shuttering to be fixed. Thus require lot of site space and skilled labour.

### Grades of Concrete:-

M10  
 ↓  
 Mix

↳ Characteristic strength  
 ( $f_{ck}$ )  $N/mm^2$

Ordinary concrete - M10 to M20

Standard concrete - M25 to M55 (For post-tensioning work)

High strength concrete - M60 to M80  
 ↓  
 (For pretensioned prestressed con.)

### Concrete making materials:-

① Cement - cement is the only chemically active ingredient of concrete which shows ~~binding~~ <sup>binding</sup> properties after reacting with water. It consists of silicates and aluminates of calcium which form a hardened mass after mixing with water. This type of cement is also known as hydraulic cement.

① ordinary portland cement -

ordinary portland cement (OPC) is commonly used in construction. The BIS has classified OPC in three grades. This is based on compressive strength of cement sand mortar cubes.

- (i) 33 grades
- (ii) 43 grades
- (iii) 53 grades.

here the grade no. indicates the minimum compressive strength of cement-sand mortar cubes in  $N/mm^2$  at 28 days.

- (2) Rapid hardening portland cement
- (3) Low heat portland cement
- (4) portland slag cement
- (5) Sulphate Resisting cement
- (6) portland pozzolona cement
- (7) White cement.

(2) Aggregate:- The bulk of concrete is made up of aggregate. Aggregate are inert material or chemically inactive material like crushed rock, sand broken bricks, gravel etc. Aggregate, less than 4.75mm size are known as fine aggregate and which are more than 4.75mm size are known as coarse aggregate.

Coarse aggregate gives strength to concrete and fine aggregates acts as a filler but the coarse agg. and provides workability to the concrete mix.

(3) Water:- Water is required for chemical reaction of cement and also for providing workability to concrete. The water is used for mixing and curing of concrete should be clear and free from injurious amounts of acids, alkalis, salts or other chemical substances, which can harm concrete or steel and the water cement ratio is 0.45 to 0.55 and it is the factor for the making of the concrete.

Properties of Concrete: - The properties of concrete depend upon the properties and proportions of its ingredients.

① Compressive strength: - The characteristic <sup>compressive</sup> strength of concrete is defined as the compressive strength of 15 cm cubes at 28 days in M.M.F, below which not more than 5% of the test results are expected to fall. It is represented as  $f_{ck}$  and it is determined by cube test.

$$f_M = f_{ck} + 1.64\sigma$$

$\sigma$  = standard deviation

$\sigma = \sqrt{V}$       $V \rightarrow$  Variate

$f_M$  = Mean strength has 50% probability that strength of concrete is not exceeded by  $f_M$ .

② Workability: - The workability of concrete is defined as the ease by which it can be mixed, placed, compacted and placed and finished. A workable concrete should not bleed or segregate. It depends on the following factors:

- (i) Water cement ratio
- (ii) Size of aggregate
- (iii) Shape of aggregate
- (iv) Ratio of fine to coarse aggregate

Workability can be measured by following tests:

- (i) Slump test
- (ii) Vee-Bee Consistometer test
- (iii) Compaction factor test.

③ Durability: - The concrete should be durable to the environment it is exposed to, during its life. The main characteristic of durability is its permeability to the ingress of water, oxygen, carbon dioxide, chloride sulphate etc.

④ Tensile strength: - The tensile strength of concrete can be correlated with the characteristic compressive strength of concrete. IS 456 gives the following correlation

$$\left. \begin{array}{l} \text{tensile} \\ \text{strength} \end{array} \right\} f_{tc} = 0.7 \sqrt{f_{ck}} \left. \vphantom{\begin{array}{l} \text{tensile} \\ \text{strength} \end{array}} \right\} \text{N/mm}^2$$

⑤ Modulus of Elasticity: - The short term static modulus of elasticity can be expressed in terms of the characteristic compressive strength and may be:

$$\left\{ E_c = 5000 \sqrt{f_{ck}} \right\}$$

long term modulus of elasticity ( $E_{cc}$  or  $E_{ct}$ ):

$$E_{cc} \text{ or } E_{ct} = \frac{E_c}{1 + \alpha} \quad (\alpha = \text{creep coefficient})$$

⑥ Poisson's Ratio: - Poisson's ratio is defined as the ratio of lateral strain to the longitudinal strain. It varies from 0.1 to 0.3 for concrete.

⑦ Creep: - Creep is caused under sustained loading. It is seen that when concrete is subjected to sustained loading, strain keeps  $\uparrow$  with time, even without any  $\uparrow$  in the load.

⑧ Shrinkage: - Concrete shows shrinkage due to loss of moisture by evaporation. Shrinkage also causes strain in concrete.

⑨ Freezing & Thawing: - If freezing & thawing conditions exist, then durability of concrete should be enhanced by adding suitable air entraining admixtures.

⑩ Sulphate attack: - Concrete exposed to sulphate attack such as in coastal environment, should be made from sulphate resisting cement.

in IS 456 (Table 1.4) gives recommendations regarding the type of cement.

Concrete mix proportioning: - The determination of the proportions of cement, aggregates and water to attain the desired strength and properties such as workability, durability etc. is called the concrete mix proportioning. (6)

design of concrete mix is classified into following two types by IS:456:2000 (clause 9)

- I. Nominal mix concrete
- II. Design mix concrete

① Nominal mix concrete: - A concrete mix in which the proportions of cement, aggregate and water are adopted is called as nominal mix. It is not necessary that such a mix will give the desired strength and properties. For ex. M15 is 1:2:4. Nominal mix is not used for grades higher than M20. It is used for ordinary concrete only.

② Design mix concrete: - The concrete obtained by properly determining the proportions of the ingredients of concrete to get the concrete of desired strength & properties is called as design mix concrete.

$$f_{cm} = f_{ck} + 1.65 \sigma$$

$\uparrow$  standard deviation  
 $\downarrow$  characteristic strength

↓ mean target strength

mixes of grades

M10 - 1:3:6

M15 - 1:2:4

M20 - 1:1.5:3

M25 - 1:1:2 → aggregate

$\downarrow$  cement       $\downarrow$  sand

Design philosophies :- Design of any R.C.C. member

comprises of the following-

- ① To decide the size of the member and the amount of reinforcement required
- ② To check whether the adopted section will perform safely and satisfactorily during the life time of the structure

Various methods used for the design of R.C.C member-

- I. working stress method
- II. load factor or ultimate load method
- III. limit state method

① working stress method :- This method of design was oldest method. It is based on the elastic theory and assumes that both steel and concrete are elastic and obey Hooke's law. It means that the stress is directly proportional to the strain up to the point of collapse.

On this method, the ultimate strength of concrete and yield strength of concrete or 0.2% proof stress of steel are divided by factors of safety to obtain permissible stress

II. load factor method or ultimate load method :- In this method, ultimate or collapse load is used as design load. The ultimate load are obtained by increasing the working / service loads suitably by some factors. These factors which are multiplied by the working load to obtain ultimate loads are called as load factors.

$$\text{Load factor} = \frac{\text{Collapse load}}{\text{Working load}}$$

This method used the real stress-strain curve of concrete

③ Limit state method :- This is the most rational method which takes into account the ultimate strength of structure and also the serviceability requirements. It is a judicious combination of working stress & ultimate load method of design. The acceptable limits of safety & serviceability requirements before failure occurs is called a limit state.

Two imp. limit states to be considered in design are:

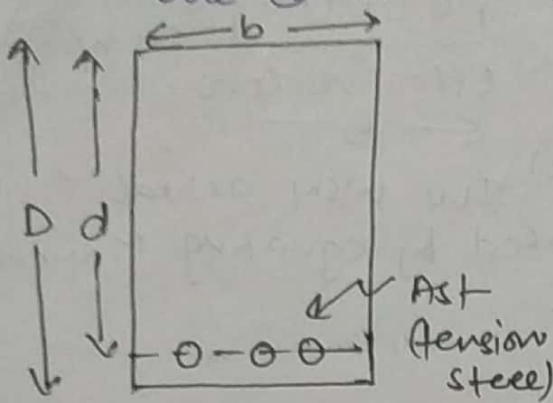
- I. Limit state of collapse
- II. Limit state of serviceability



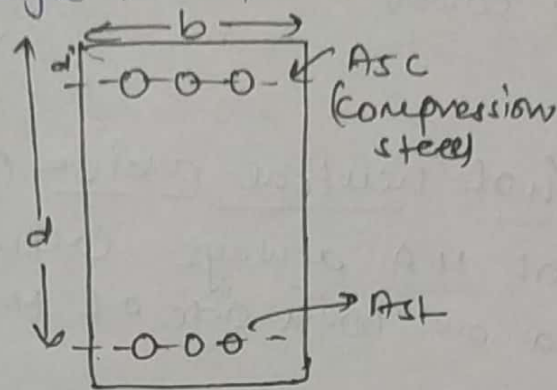
Types of R.C.C. Beams:- R.C.C. beams are of following

Three types:-

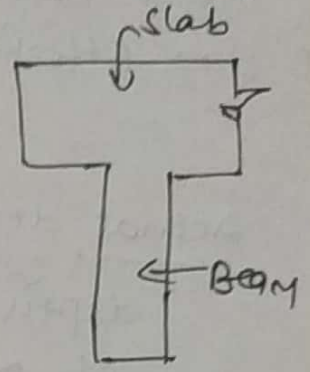
(I) Single reinforced Beams:- The beams in which steel reinforcement is placed in the tensile zone only are called as single reinforced beams.



I. Singly reinforced beam



II. Doubly reinforced beam



III. T-beam

(II) Doubly reinforced beam:- The beams in which reinforcement is placed in the tensile as well as compression zone are called as doubly reinforced beam.

(III) Flanged beams (T beams & L beams):- In most reinforced concrete structures, the slab and beams are cast monolithically. Thus the beam forms a part of the floor system.

Modular ratio:- It is defined as the ratio of the modulus of elasticity of steel to the modulus of elasticity of concrete.

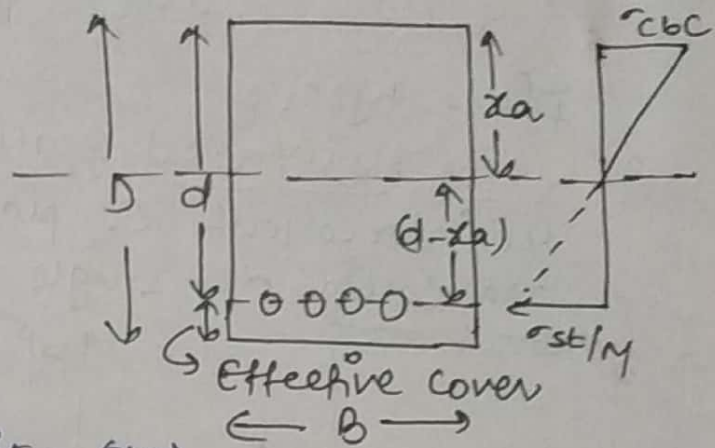
$$m = \frac{E_s}{E_c}$$

$$m = \frac{280}{3\sigma_{cbc}}$$

Grade of concrete	M15 $\sigma_{cbc}$ 5	M20 7	M25 8.5	M30 10	M35 11.5	M40 13
$m = 280/3\sigma_{cbc}$	18.67 = 19	13.33 = 13	10.98 = 11	9.33 = 9	8.17 = 8	7.17 = 7

# Single reinforced section:

- D → Overall depth
- d → effective depth
- B → effective width
- D-d → Effective cover



Actual depth of neutral axis - (xa) In wsn actual depth of N.A. always calculated by equating Moment of Area on both side of N.A.

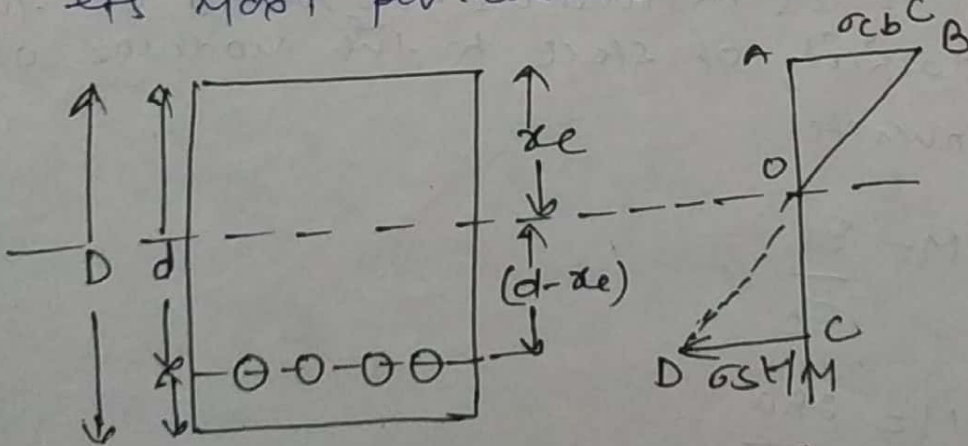
Moment of area - In compression =  $B \cdot xa \cdot \frac{xa}{2}$   
 or from C = T  $\frac{Bxa^2}{2}$

In tension =  $m A_{st} \cdot (d - xa)$

Then  $\frac{Bxa^2}{2} = m A_{st} \cdot (d - xa)$

then  $A_{st} \uparrow \Rightarrow xa \uparrow$

critical depth of neutral axis → critical depth of neutral axis is such depth of the actual neutral axis for which stress in concrete & steel are attained its max permissible value at the same time.



From similar  $\Delta$   
 $\frac{\sigma_{cbc}}{xe} = \frac{\sigma_{st}/M}{(d - xe)}$   
 $d = \frac{\sigma_{st} + M \sigma_{cbc}}{M \sigma_{cbc}}$

$xe = \left( \frac{M \sigma_{cbc}}{\sigma_{st} + M \sigma_{cbc}} \right) d$

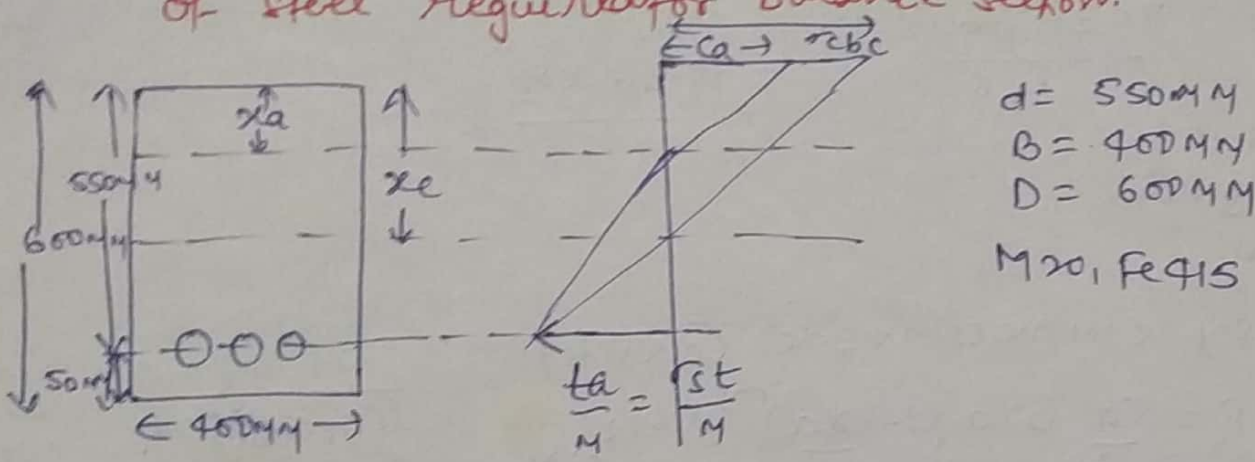
$xe = kd$

$k = \frac{M \sigma_{cbc}}{\sigma_{st} + M \sigma_{cbc}}$

$k = \frac{M C}{t + M C}$

$\sigma_{cbc} = c$   
 $\sigma_{st} = t$

Que: Find out MOR of an RCC Beam section of size 450x600mm  
 M20 concrete and Fe 415 steel used. used WSM and effective  
 cover 50mm, area of steel (i) 3 NOS 16MM dia( $\phi$ )  
 (ii) 4 NOS 25MM  $\phi$  dia)  
 (iii) Calculate MOR of the balance section and find out area  
 of steel required for balance section.



(i) 3 NOS 16MM  $\phi$  (dia.)

↳ 3 bars of 16MM  $\phi$  (dia.)

area of steel  $A_{st} = 3 \times \frac{\pi}{4} \times (16)^2 = 603.185 \text{ MM}^2$

Step:1. to find actual depth ( $x_a$ )

$$\frac{B x_a^2}{2} = m A_{st} (d - x_a)$$

$$450 \frac{x_a^2}{2} = 13 \times 603.185 (550 - x_a)$$

$$\Rightarrow 200 x_a^2 = 13 \times 603.185 (550 - x_a)$$

$$x_a = 128.5456 \text{ MM}$$

Step:2 To find critical depth ( $x_c$ )

$$\frac{x_e = kd}{t = 230}$$

$$k = \frac{MC}{t + MC} = \frac{13 \times 7}{230 + 13 \times 7}$$

$$k = 0.2834$$

$$x_e = kd = 0.2834 \times 550$$

$$= 155.9190$$

$$\approx 156 \text{ MM}$$

$x_a < x_e$

So this section is under reinforced section.

MOR from tension side (steel)

$$MOR = t_{st} A_{st} (d - x_a/3)$$

$$t_{st} = 230$$

$$MOR = 230 \times 603.185 \left( 550 - \frac{128.54}{3} \right) \text{ KN}\cdot\text{MM} \quad \begin{matrix} Fe415 \\ P181 \\ T122 \end{matrix}$$

$$e_u \text{ under} = \frac{70358675.17}{10^6}$$

$$\text{reinforced section steel at the yield value} = \frac{70.36 \text{ KN}\cdot\text{M}}{10^6}$$

MOR from compression side (concrete)

$$MOR = \frac{c_a}{2} b x_a (d - \frac{x_a}{3}) \text{ lever arm} \quad \begin{matrix} T121 \\ (c_a, \sigma_{cbc}) \end{matrix}$$

from similar triangle  $\frac{c_a}{x_a} = \frac{\sigma_{st}}{(d - x_a)}$

$$\sigma_{st} = 230$$

for Fe415

$$c_a = \frac{x_a}{(d - x_a)} \frac{\sigma_{st}}{M} = \frac{128.54}{(550 - 128.54)} \frac{230}{13}$$

$$c_a = 5.395 \text{ N/mm}^2$$

$$MOR = \frac{5.395}{2} \times 400 \times 128.54 \left( 550 - \frac{128.54}{3} \right) \text{ KN}\cdot\text{MM}$$

$$= 70339459.13 \text{ KN}\cdot\text{MM}$$

$$= \frac{70.3339 \text{ KN}\cdot\text{M}}{10^6}$$

For

(iii) MOR for balanced section - ( $x_a = x_e$ )

$$MOR = Q b d^2$$

$$Q = \frac{1}{2} \sigma_{cbc} J k$$

$$MOR = 0.897 \times 400 \times 550^2$$

$$J = (1 - k/3)$$

$$MOR = 108584553 \text{ KN}\cdot\text{MM}$$

$$k = \frac{M_c}{t + M_c} = 0.283$$

$$MOR = \frac{108.58 \text{ KN}\cdot\text{M}}{10^6}$$

$$J = 0.906$$

$$\sigma_{cbc} = \frac{20}{3} = 7$$

$$Q = 0.8973$$

Find out area of steel of balanced section

$$MOR = \sigma_{st} A_{st} (d - x_a/3)$$

$$x_a = x_e \quad \text{For (Balancing)}$$

$$MOR = \sigma_{st} A_{st} d (1 - k/3)$$

$$MOR = \sigma_{st} A_{st} Jd$$

$$108.58 \times 10^6 \text{ N}\cdot\text{mm} = 230 \times A_{st} \times 0.906 \times 550$$

$$A_{st} = \underline{\underline{947.43 \text{ mm}^2}}$$

# Doubly Reinforced section (Beam) :- $M.R = Q B d^2$

Que:- A Rectangular Beam over all  $x$ -section  $230 \times 600$  mm and effective cover  $50$  mm is reinforced  $5$  Nos  $25\phi$  (dia) bars on tension side,  $3$  Nos  $16\phi$  bars on compression side it is carrying an imposed load of  $50$  kN/m over an effective span of  $7$  m.  
 permissible stress in steel  $\sigma_{st} = 230$  N/mm<sup>2</sup> &  
 " " " Concrete  $\sigma_{cb} = 7$  N/mm<sup>2</sup>

$m = 15$  check the adequacy of the section. ?

Self weight = density  $\times$  area  $\rightarrow 25$  kN/m<sup>2</sup>

$= 25 \times 230 \times 0.6 = 3.45$  kN/m

Total load = self load + imposed load  
 $= 3.45 + 50 = 53.45$  kN/m

span =  $7$  m

$B.M = \frac{w l^2}{8} = \frac{53.45 \times 7^2}{8} = 327.38$  kN.m

$x_e = kd$   $k = \frac{mC}{f + mC} = \frac{15 \times 7}{230 + 15 \times 7}$

$D = 600$   $k = 0.3134$

$d_c = 50$

$d = 550$

$x_e = 172.38$  mm

For  $x_a$  equate the MOA from tension & compression side

$\frac{B x_a^2}{2} + (1.5m - 1) A_{sc} (x_a - d_c) = m A_{st} (d - x_a)$

$230 \times \frac{x_a^2}{2} + (1.5 \times 15 - 1) A_{sc} (x_a - 50) = 15 \times A_{st} (550 - x_a)$

$A_{sc} = 3 \times \frac{\pi}{4} \times 16^2$   $A_{st} = 5 \times \frac{\pi}{4} \times 25^2$

$x_a = 261.63$  mm

So  $x_a > x_e$  Over reinforced section

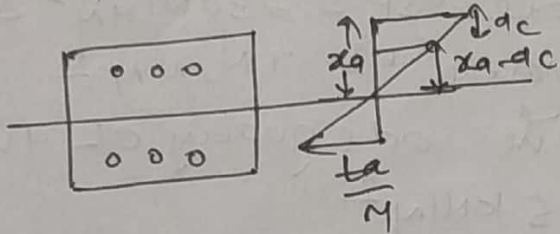
$$c_a = \sigma_{cbc} = \gamma$$

$$t_a c \sigma_{st}$$

use compression side (Concrete failure)

$$MOR = \frac{c_a}{2} B x_a \left( d - \frac{x_a}{3} \right) + (1.5M-1) A_{sc} c' (d - d_c)$$

For  $d'$  use similar triangle



$$\frac{c'}{x_a - d_c} = \frac{\sigma_{cbc}}{x_a}$$

$$c' = 5.666$$

$$MOR = 134.184 \times 10^6 \text{ N}\cdot\text{m}$$

$$= 134.184 \times 10^6 \text{ N}\cdot\text{m}$$

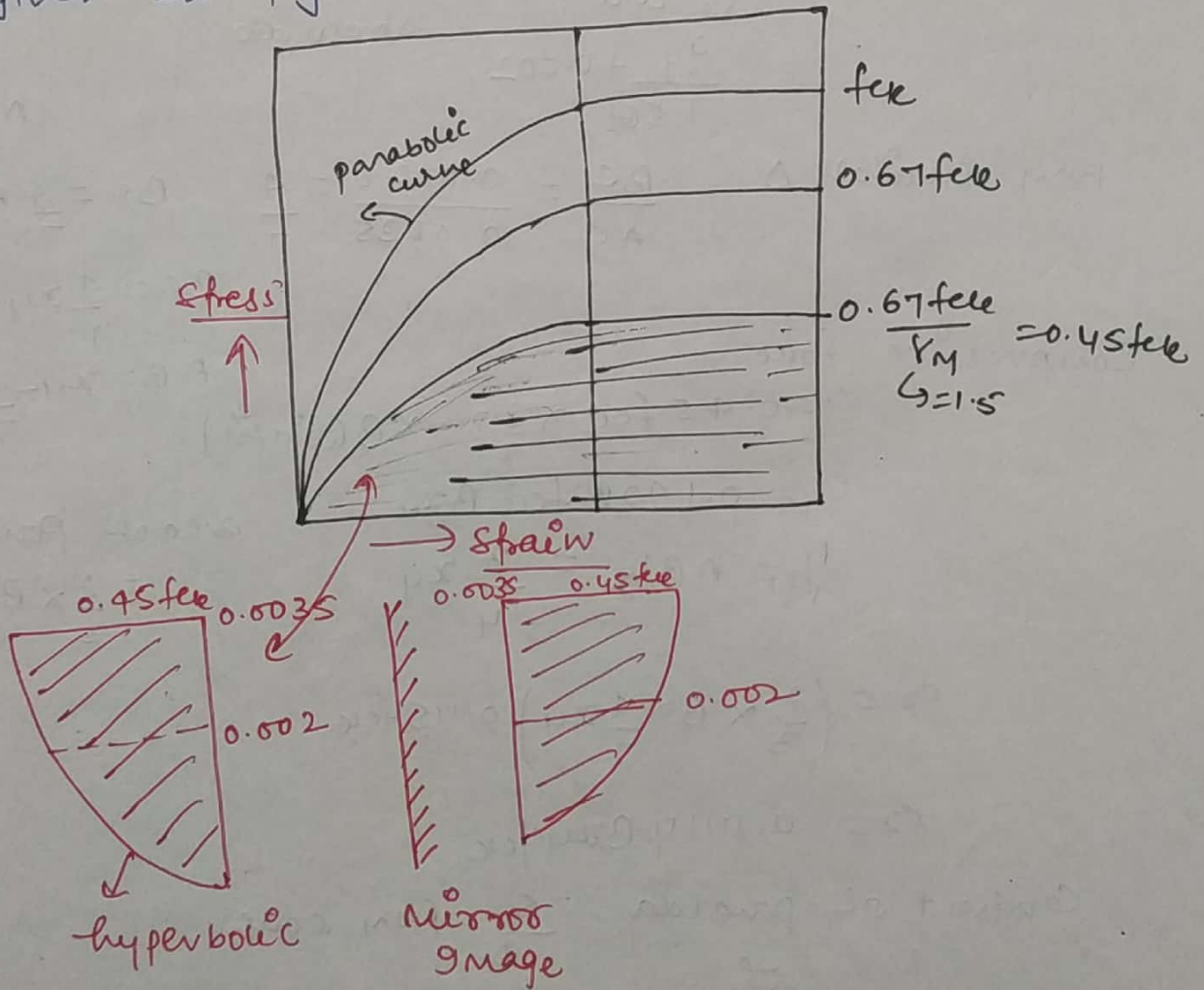
$$\text{So } MOR = 134.184 \text{ N}\cdot\text{m}$$

$BM > MR$  so section is not safe. Ans.

Limit state method  
(ultimate load theory)

Assumptions in limit state design:

- (i) plane section before bending remain plane after bending. or means strain diagram is linear
- (ii) Max strain in outer most compression fiber in bending equal to 0.0035.
- (iii) An acceptable stress strain curve for a concrete is given in figure.



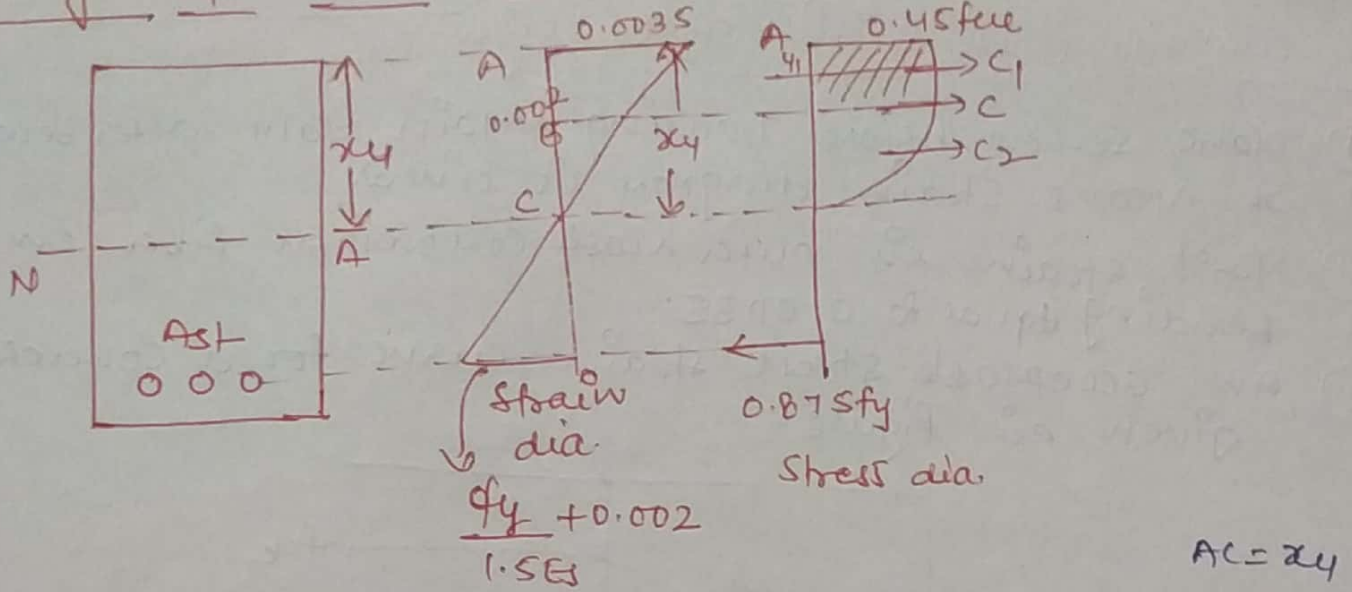
IV. Tensile stress of concrete is ignore.

V. max strain in tension reinforcement in the section at failure shall not be less than  $\left[ \frac{f_y \times E_s + 0.002}{1.15} \right]$   
 "  $\frac{0.875 f_y}{E_s} + 0.002$



VI. Permissible stress in concrete is considered 67 times of characteristic & partial F.O.5 also considered.

Analysis of stress strain curve:-



From similar  $\Delta$   $\frac{BC}{AC} = \frac{0.0020}{0.0035} = \frac{4}{7}$   $BC = \frac{4}{7} AC$

$BC = \frac{4}{7} x_u$

$AB = x_u - \frac{4}{7} x_u = \frac{3}{7} x_u$

Compressive force

$C_1 = 0.45 f_{ck} \times \frac{3}{7} x_u \times B$  (width)

$C_1 = 0.1928 f_{ck} B x_u$

$y_1 = AB/2 = \frac{3}{14} x_u$

area of parabola  $= \frac{2}{3} \times \text{Base} \times \text{height}$

$C_2 = \left( \frac{2}{3} \times B \times \frac{4}{7} x_u \right) 0.45 f_{ck}$

$C_2 = 0.1714 B x_u f_{ck}$

Centroid of parabola  $= \frac{5}{8}$  from lower

where  $c_2$  act  $\rightarrow 3/8$  from top

$y_{c2} = 8 \times \frac{3}{7} x_u + \frac{3}{8} \times \frac{4}{7} x_u$   $y_{c2} = \frac{9}{14} x_u$

Total compressive force  $C = C_1 + C_2$

$= 0.1928 f_{ck} B x_u + 0.1714 B x_u f_{ck}$

$C = 0.3642 f_{ck} B x_u$

Lever arm  $\rightarrow$  distance b/w compressive force & tensile force

$$\bar{y} = \frac{C_1 y_1 + C_2 y_2}{C_1 + C_2} = \frac{.1928 \text{ fee } Bx_4 * \frac{3}{14} x_4 + .1714 \text{ fee } Bx_4 * \frac{9}{14} x_4}{0.3642 \text{ fee } Bx_4}$$

$$\bar{y} = .416x_4$$

$$\bar{y} = \underline{0.42x_4}$$

Tensile force  $\left\{ T = 0.87 f_y A_{st} \right\}$

$$L.A. (\text{Lever arm}) = (d - \bar{y})$$

$$\left\{ L.A. = d - 0.42x_4 \right\}$$

MOR  $\rightarrow$   $MR = \text{compressive force} \times L.A.$

$$\left\{ MR = 0.36 \text{ fee } Bx_4 (d - 0.42x_4) \right\}$$

$$MR = \text{Tensile force} \times L.A.$$

$$\left\{ MR = 0.87 f_y A_{st} (d - 0.42x_4) \right\}$$

$$\underline{P196/c}$$

Actual depth of N.A. ( $x_4$ )  $\rightarrow$

$$C = T$$

$$0.36 \text{ fee } Bx_4 = 0.87 f_y A_{st}$$

$$\left\{ x_4 = \frac{0.87 f_y A_{st}}{0.36 \text{ fee } B} \right\}$$

$$\underline{P196/c}$$

Limiting depth of N.A. ( $x_{4 \text{ limiting}}$ )  $\rightarrow$

$$x_{4 \text{ lim}} = \left( \frac{700}{(0.87 f_y + 1100)} \right) d$$

$$K = 700$$

$$x_{4 \text{ lim}} = Kd$$

$$0.87 f_y + 1100$$

For  $f_c = 250$

$$K = 0.53$$

$f_c = 15$

$$K = 0.979 \approx 0.98$$

Que: Calculate the MOR of RCC Rectangular section  
use M20 & Fe415.

(i) 4 Nos - 16  $\phi$  (MM dia)

(ii) 6 Nos - 25  $\phi$  (MM dia)

(iii) Calculate Ast just required for limiting section.  
Rectangular Beam of 600 x 400 MM and effective  
cover of 50 MM.  $D = 600$  MM,  $B = 400$  MM.

(i) For  $x_u$   $C = T$   $f_y = 415$   
 $f_{ck} = 20$

$$4 \text{ Nos} - 16 \phi \quad x_u = \frac{0.87 f_y A_{st}}{0.36 f_{ck} B}$$

$$A_{st} = 2412.743 \text{ mm}^2 \quad x_u = 100.82 \text{ mm}$$

For  $x_{u,lim} = k_d$   $k = 0.48$  for Fe415

$$x_{u,lim} = 264 \text{ mm}$$

$x_u < x_{u,lim}$  under reinforced section

For compression

$$M_R = 0.36 \times 20 \times 400 \times 100 \times B_2 (550 - 0.42 \times 100.82)$$

$$M_R = 147.105 \times 10^6 \text{ N/mm} \underline{mm}$$

For Tension

$$M_R = 0.87 f_y A_{st} (d - 0.42 x_u)$$

$$= 0.87 \times 415 \times 2412.75 (550 - 0.42 \times 100.82)$$

$$M_R = 147.410 \times 10^6 \text{ N.mm}$$

Ans.

(ii) 6 Nos - 25  $\phi$

$$A_{st} = 6 \times \frac{\pi}{4} \times 25^2$$

$$= 294534 \text{ mm}^2$$

$$x_u = \frac{0.87 f_y A_{st}}{0.36 f_{cc} B}$$

$$x_u = \underline{369.228 \text{ mm}}$$

$$x_{u,lim} = kd$$

$$= 0.48 \times 550$$

$$\underline{x_{u,lim} = 264 \text{ mm}}$$

$$x_u > x_{u,lim}$$

So over reinforced section

$$M_R = 0.36 f_{cc} B x_{u,lim} (d - 0.42 x_{u,lim})$$

$$= 0.36 \times 20 \times 400 \times 264 (550 - 0.42 \times 264)$$

$$M_{u,lim} = M_R = \underline{333.87 \times 10^6 \text{ N}\cdot\text{mm}}$$

Ans.

(iii) Ast for the limiting section

$$A_{st} = \frac{B.M.}{0.87 f_y d J}$$

$$J = (1 - 0.42k)$$

$$J = (1 - 0.42 \times 0.48)$$

$$\underline{J = 0.7984}$$

$$M = \underline{333.87 \times 10^6}$$

$$A_{st} = \underline{2105.84 \text{ mm}^2}$$

or II<sup>nd</sup> method

$$C = T$$

$$0.36 f_{cc} B x_{u,lim} = 0.87 f_y A_{st}$$

$$A_{st} = \underline{2105.84 \text{ mm}^2}$$

Ans.

## Doubly reinforced section:-

Que. Size of RC beam is restricted to 250mm x 500mm of carrier a super impose load of 25 kN/m over a span of 6m determine the reinforcement for a beam of by LSM use M20 & Fe415 Effective cover of steel is 40mm

Soln. MOTG  $f_{yd} = \text{design strength} = 0.87 f_y$   
self weight =  $0.25 \times 0.5 \times 25$   
 $= 3.125 \text{ kN/m}$

$$W = 25 + 3.125$$

$$W = 28.125 \text{ kN/m}$$

using LSM  $W_u = 1.5 \times 28.125 = 42.1875$

$$B M_u = \frac{W_u l^2}{8} = \frac{42.2 \times 6^2}{8} = 189.9 \text{ kN.m.}$$

MOR of Balance section

$$M_R = Q B d^2$$

$$Q = 0.138 f_{ck}$$

$$M_R = 146 \text{ kNm}$$

$$Q = 2.76 \times 20 \times 10^6$$

$$B M_u > M_R$$

hence we provide doubly reinforced section  
Fe415

$$x_{u, \text{lim}} = 0.48d$$

$$d = 460$$

$$x_{u, \text{lim}} = 220.8$$

$$M_R = 0.87 f_y A_{st1} (d - 0.42 \times 220.8)$$

$$A_{st1} = 1101.05 \text{ mm}^2$$

$$A_{st2} = \frac{M_u - M_R}{0.87 f_y (d - d_c)}$$

$$M_{R2} = B \cdot M - M_{R1} = 43.9$$

$$A_{st2} = \frac{43.9 \times 10^6}{0.87 \times 415 (460 - 40)}$$

$$A_{st2} = \underline{209.4975 \text{ mm}^2}$$

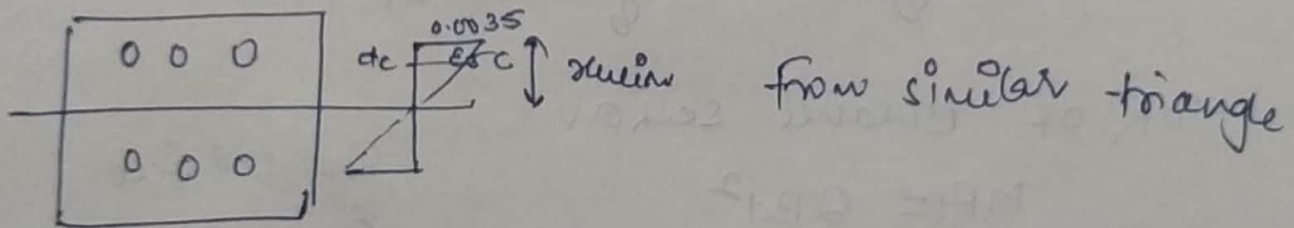
$$A_{st} = A_{st1} + A_{st2}$$

$$A_{st} = 1390.54 \text{ mm}^2$$

$$A_{sc} = \frac{M_{R2}}{(f_{sc} - 0.42 f_{ce}) (d - d_c)}$$

eu strain diagram

$$x_u = x_{u,lim}$$



$$\frac{0.0035}{x_{u,lim}} = \frac{\epsilon_{sc}}{(x_{u,lim} - d_c)}$$

$$\epsilon_{sc} = 0.0028659$$

strain	stress
0.00276	→ 352
0.00286	→ $f_{sc}$ 361
0.00380	—

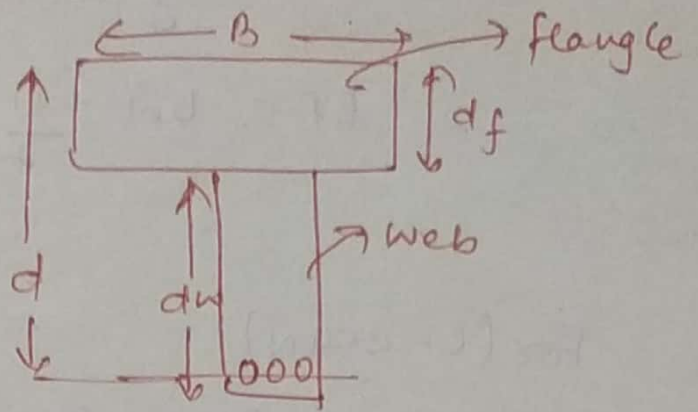
$$f_x = 352 + \frac{(361 - 352) \times (0.00286 - 0.00276)}{(0.00380 - 0.00276)}$$

$$f_{sc} = 352.86 \text{ N/mm}^2$$

$$M_{R2} = (f_{sc} - 0.42 f_{ce}) A_{sc} (d - d_c)$$

$$A_{sc} = \underline{303.97 \text{ mm}^2}$$

## T-Beam / L-Beam



### Effective width of flange:-

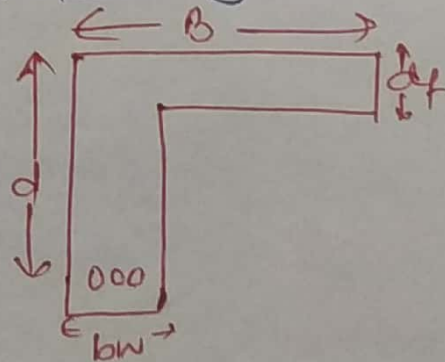
① For Isolated Beam - T Beam

$$B_f = \frac{l_o}{(l_o/B + 4)} + b_w$$

② For Isolated Beam - L Beam

$$B_f = \frac{0.5 l_o}{(l_o/B + 4)} + b_w$$

☆ if  $B_f > B$  then  $B_f$  is taken as  $B$



Pg/37 -  $l_o$  is the effective span

For Isolated beam  $\rightarrow l_o =$  effective span

NOTE:- continuous beam  $l_o$  may be assumed 0.7 of the effective span.

Pg/37 For Continuous Beam:- (For T-Beam)

$$B_f = \frac{l_0}{6} + b_w + 6d_f$$

$$B_f = b_w + \frac{l_1}{2} + \frac{l_2}{2}$$

$\left. \begin{array}{l} \text{ei} \\ \text{Both} \\ \text{min.} \\ = B_f \end{array} \right\}$

For T-Beam

For (L-Beam)

$$B_f = \frac{l_0}{12} + b_w + 3d_f$$

or

$$B_f = b_w + \frac{l_1}{2}$$

$\rightarrow$  min<sup>m</sup> of  
both  $B_f$

(For L-Beam)

$l_1 =$  clear distance

