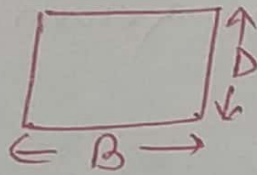


Unit - III (Column)

①

A structural element subjected predominantly to compressive force with or without bending moment is termed as "compression member". When a compression member is vertical is called a "column" and when inclined or horizontal, it is termed as "strut".

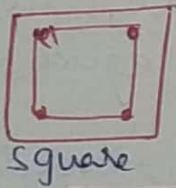
Column or strut in a compression member the effective length of is exceeded 3 times least lateral dimensions.



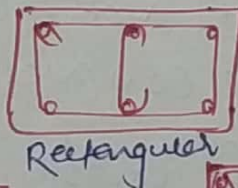
$$l_{eff} > 3(B \text{ or } D)$$

↓
Effective length

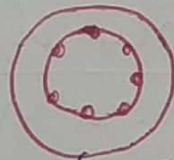
Types of column: - ① on the basis of shape of cross-section:



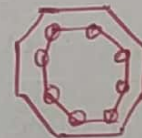
square



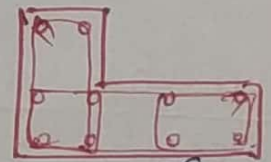
Rectangular



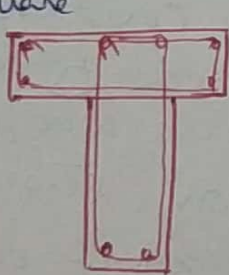
circular



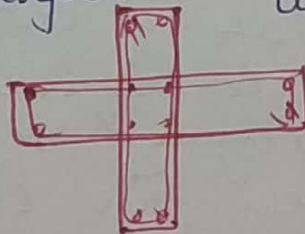
octagonal



L-shaped



T-shaped



cross-shaped

② on the basis of slenderness ratio

① short column

$$S.R. = \frac{l_{eff}}{\text{least lateral dim.}}$$

$$S.R. = \frac{l_{eff}}{B \text{ or } D} < 12$$

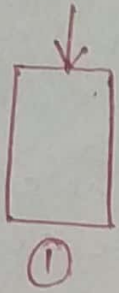
l_{eff} = Eff. length
S.R. = slenderness ratio.

② long column

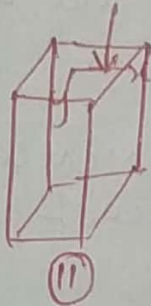
if $S.R. \geq 12$ then known as a long column.

③ on the Basis of Types of loading

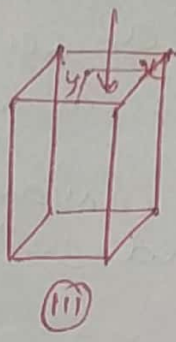
- I. Axially loaded column
- II. Uniaxially eccentrically loaded column
- III. Biaxially eccentrically loaded column



①



②



③

4. on the Basis of pattern of lateral Reinforcement

- I. Tied column
- II. Spiral column
- III. Composite column
- IV. In filled column

all the assumption discuss for the beam valid for a column also.

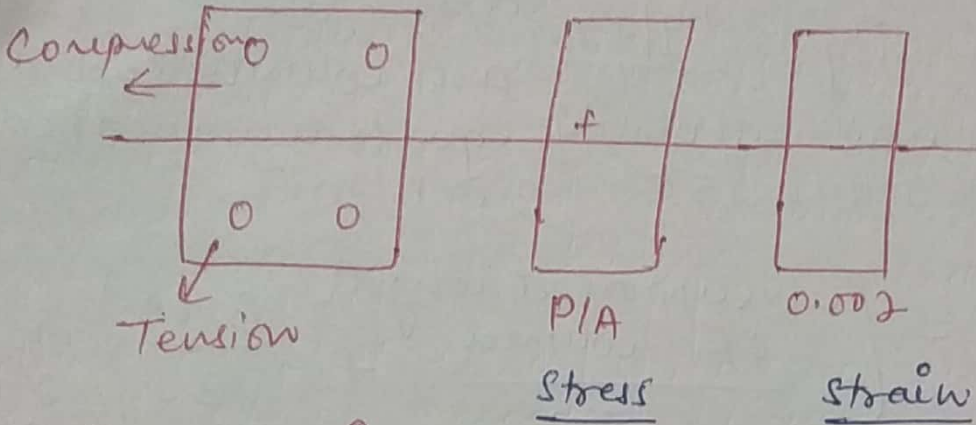
Assumptions in the column:-

- ① Max^m compression strain in concrete in axial compression equal to 0.002.
- ② Max^m compression strain at the highly compressed extreme fibre in concrete is subjected to axial compression and bending and bending when there is no tension in the section shall be equal to $= 0.0035 - 0.75 \times$ strain of least at least compressed extreme fibre.

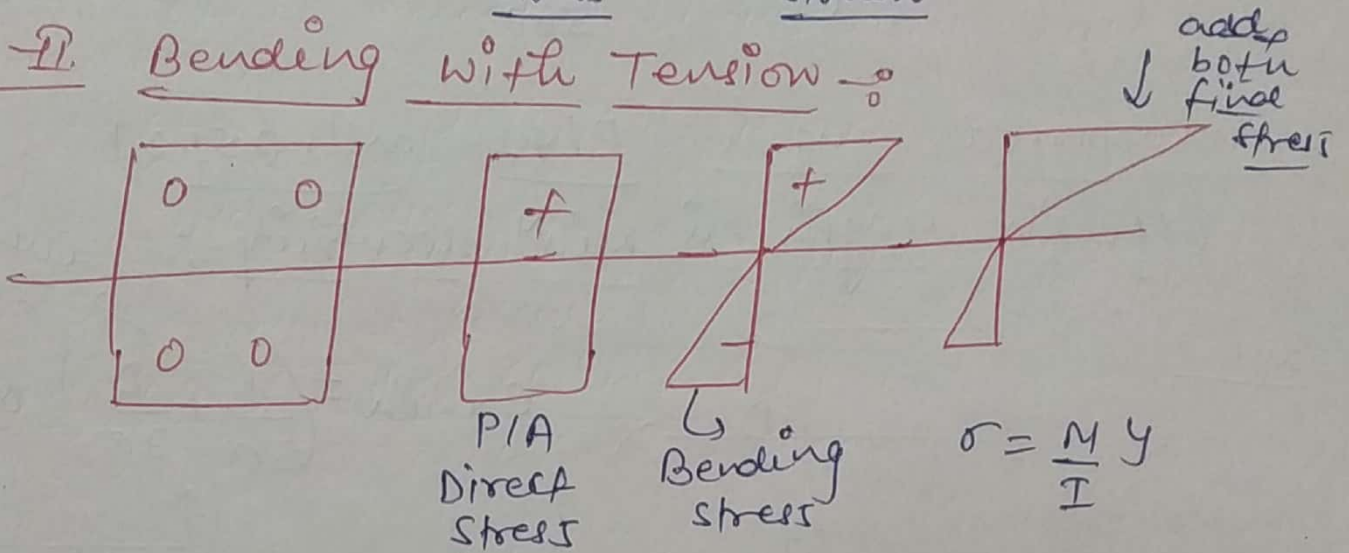
Functions of the longitudinal Reinforcement and transverse reinforcement.

- longitudinal rein. to shear the vertical compress. load, thereby the overall size of the column
- To prevent sudden brittle failure.
- Transverse reinforcement to prevent buckling of longitudinal reinforcement.
- to hold the longitudinal reinforcement in position at the time of concreting.

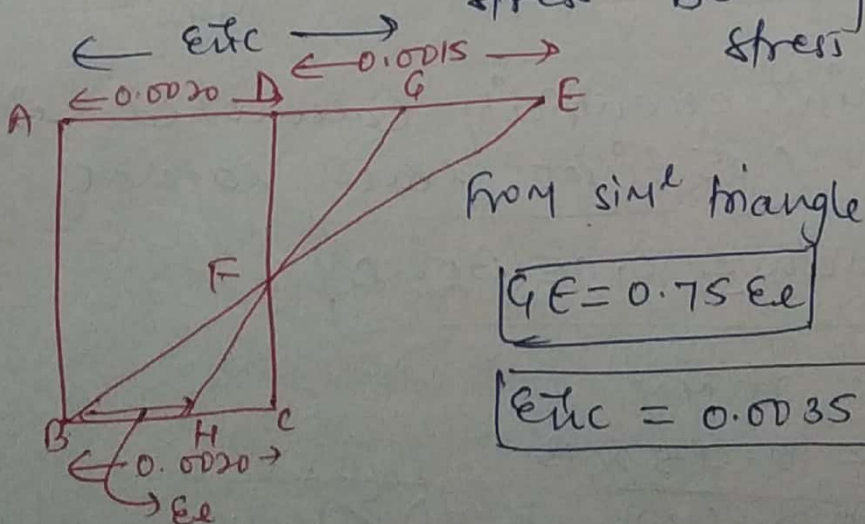
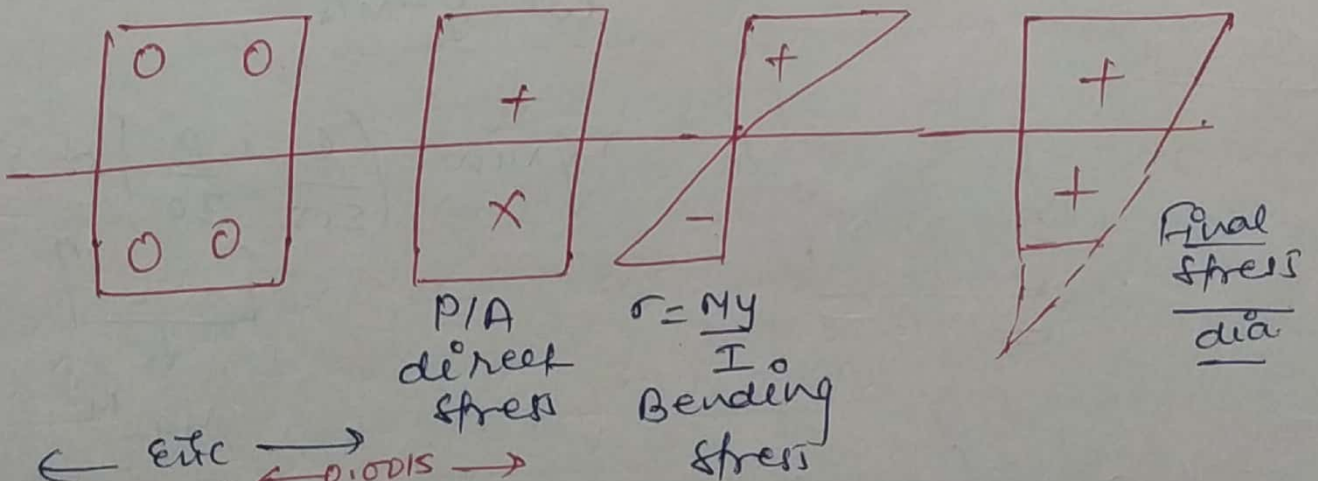
Case-I Axial Compression →



Case-II Bending with Tension →



Case-III No Tension → (Whole column compression)



Design of column

(4)

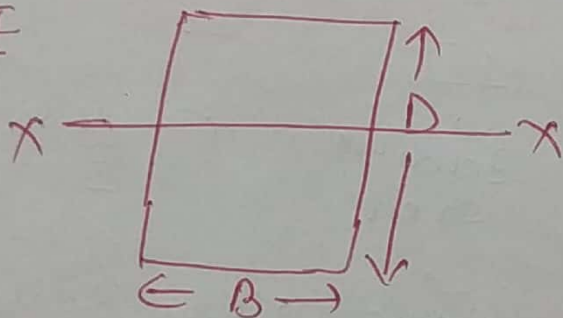
☆ min^m eccentricity → Pg/42 Art (25.4)
 design for min^m eccentricity equals unsupported length of column / 500 + B or D / 30.

$$\text{min}^m \text{ eccentricity} = \left[\frac{\text{unsupported length of column}}{500} + \frac{B \text{ or } D}{30} \right] \text{ or } 20 \text{ mm}$$

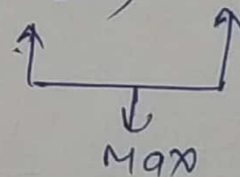
unsupported length: P/42 art. (25.3.)

Effective length e_{min} min^m eccentricity → cut e_{min} x-axis

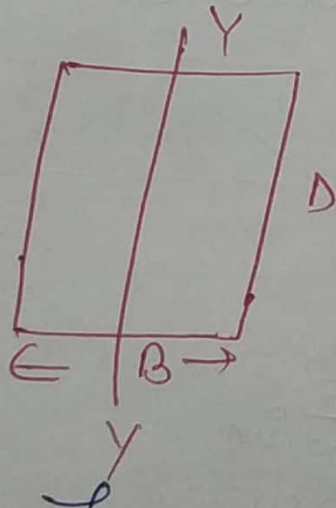
Case-I



$$e_{x \text{ min}} = \left(\frac{l}{500} + \frac{D}{30} \right) \text{ or } 20 \text{ mm}$$

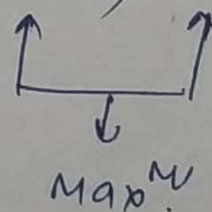


Case-II



cut y-axis

$$e_{y \text{ min}} = \left(\frac{l}{500} + \frac{B}{30} \right) \text{ or } 20 \text{ mm}$$



NOTE (i) When min^m eccentricity calculated is less than 0.05 times least lateral dimension.

$$e_{\text{min}} \leq 0.05(B \text{ or } D)$$

NOTE (ii)

$$e_{\text{min}} = 20 \text{ mm}$$

$$20 \leq 0.05 \times B$$

$$B \geq 400 \text{ or } D \geq 400$$

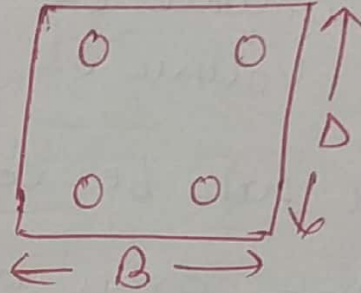
NOTE III min. size of short column = 400mm (5)

★ Design steps for short column: (pg/71)
M.M.G. When short axially for loaded column load carrying capacity of the column,

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$A_c = A - A_{sc}$$

↓ Total area
↓ area of steel in compression



A_c = area of concrete

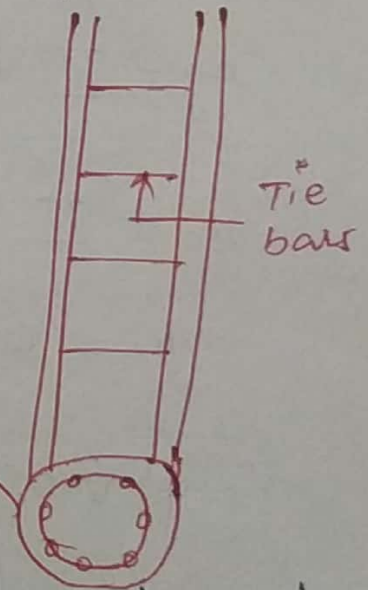
A = Total area

A_{sc} = area of steel in compression

Circular column - A) Type No. I of separate tie bars are used

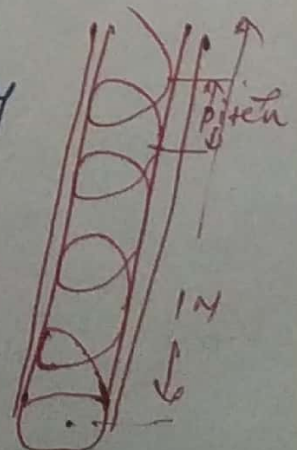
$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

Circular x-section



Type No. II with helical reinforcement (Tie bars) as a helical or helical reinforcement is used then load carrying capacity of column is ↑ by 5%.

$$P_u = 1.05 (0.4 f_{ck} A_c + 0.67 f_y A_{sc})$$



For helical reinforcement spacing should be ⑥
 such that following criteria should
 be satisfied

$$0.36 \frac{f_{ce}}{f_y} \left[\frac{A_g}{A_e} - 1 \right] \leq \left[1 \times \frac{V_{th}}{V_c} \right]$$

Pg/71

Art. 39.4.

V_{th} = Volume of helical reinforcement
 V_c = Volume of core

$\frac{V_{th}}{V_c}$ should not be less than $0.36 \left[\frac{A_g}{A_e} - 1 \right] \frac{f_{ce}}{f_y}$

A_g = gross area

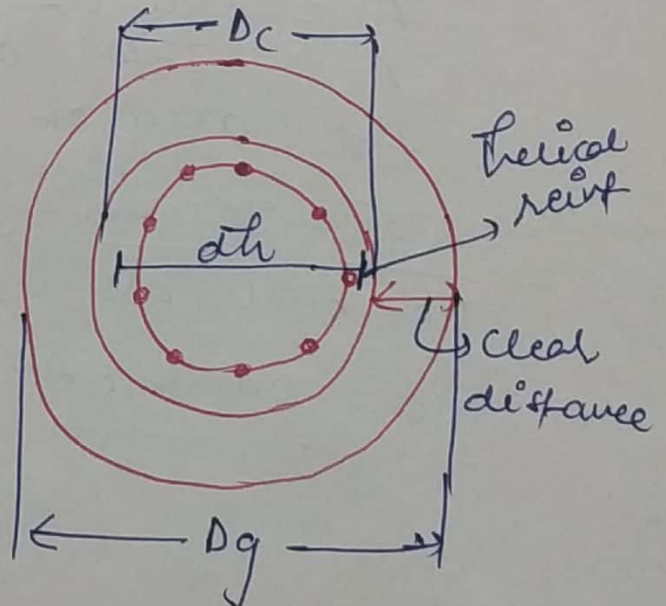
A_e = core area

$$D_c = D_g - 2 \times \text{clear cover}$$

$$A_g = \frac{\pi}{4} D_g^2$$

$$A_e = \frac{\pi}{4} D_c^2$$

D_c = core dia



V_c = volume per unit length of column

$$V_c = A_e \times 1000 \text{ mm}^3 \text{ when set the length of the column is 1M.}$$

V_{th} = volume of helical reinforcement in one unit length of column (say 1M.)

V_{th} = no. of turns \times length of one turn \times cross-sectional area of helical reinforcement.

$\Rightarrow \phi_h = \text{dia of helical reinforcement}$

(7)

$\Rightarrow \text{no. of turns} = \frac{1000}{p}$ when length 1m

$p \rightarrow \text{pitch}$

$$d_h = d_c - \frac{\phi_h}{2} - \frac{\phi_h}{2} = d_c - \phi_h$$

length of one turn = $\pi d_h = 2\pi \frac{d_h}{2}$ \rightarrow radius

so $\left\{ V_h = \frac{1000}{p} \times \pi d_h \times \frac{\pi}{4} \phi_h^2 \right\}$

$\left\{ V_c = A_c \times 1000 \right\}$

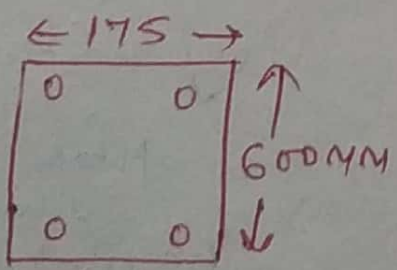
Some IS recommendation: $\frac{p}{4\phi_h}$ min % of steel = 0.8% of gross area

- \rightarrow Max % of steel 1) when bars are not lap = 6%
- ii) when bars are lap = 4% (of gross area)

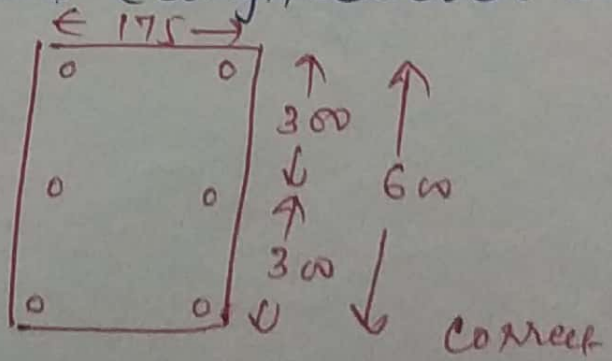
\rightarrow min dia. of bar = 12mm

\rightarrow min no. of bars \rightarrow circular = 6 bars
 Rectangular = 4 bars

\rightarrow Max spacing = 300mm
 of main bars (longitudinal bars)



X
 WRONG



Transverse Reinforcement (Tie bars or stirrups) (8)

Pg/48

Diameter ->

i) $\frac{\phi_{main}}{4}$
or
6mm

max.

P/48

Spacing ->

distance bet
two bars

i) least lateral dimension
(B or D)

ii) $16 \times \phi_{main}$

iii) 300mm.

min. of
all

P/49. Pitch of Helical Reinforcement :-

i) Not greater than 75mm ($\nless 75mm$)

ii) Not less than 25mm ($\nless 25mm$)

iii) $\nless \frac{1}{6} \times D_c$

iv) $\nless 3 \phi_{th}$

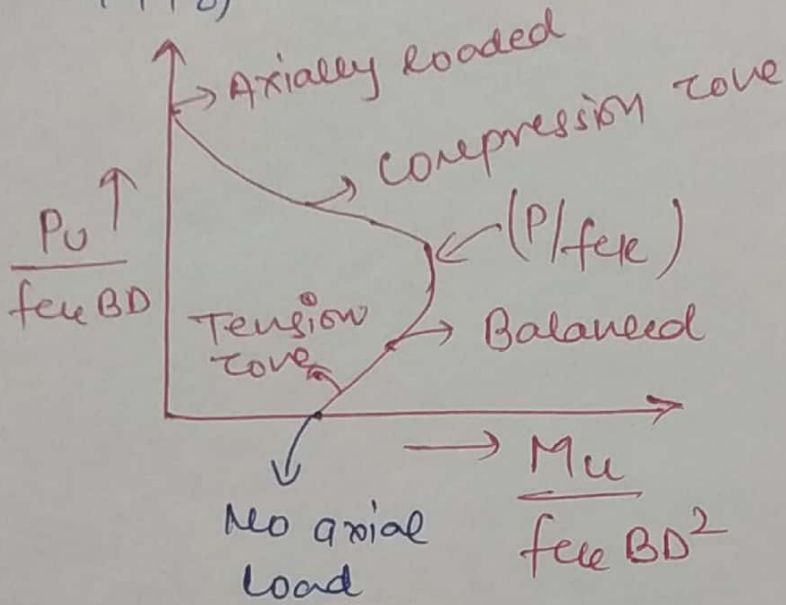
min.
of all

that
would
be the
pitch of the
helical reinforcement

Design of column subjected to axial load and bending

1) P-M Interaction chart (special publication HP-16)

Book - (Design AIDS for Reinforced Concrete (IS 456-1978))



- i) $M_u = 0$
→ axially loaded
- ii) $P_u = 0$
Pure bending
- iii) P_u & M_u Both are present

- i) of a column is to design for a load P_u and moment M_u
- ii) size of the column should be known (B x D)
- iii) chart - given

Step-I Find out value of $P_u / f_{ck} \cdot B \cdot D = Y_{value}$

Step-II Find out value of $M_u / f_{ck} \cdot B \cdot D^2 = X_{value}$

Step-III As per value of X & Y from the interaction chart we can find $P / f_{ck} = k$.

Step-IV % of steel required = p ($P = k \cdot f_{ck}$)
Area of steel required $A_{st} = \frac{p \times B d}{100}$

Step-V ultimate load carrying capacity of the column (P_{uz}) when (moment = 0) as per code IS: 456 2000 (Pg 171) (10)

$$P_{uz} = 0.45 f_{cc} A_c + 0.75 f_y A_{sc}$$